# Lecture 9: Sequence Alignment

- Sequence alignment and evolution

   mutations
- Edit graph & alignment algorithms
- Multiple sequence alignment
  - Higher-dimensional edit graphs
  - Progressive alignment

# *Aligning* sequences: Major uses in genome analysis

- To find relationship between sequences from "same" genome, e.g.
  - finding gene structure by aligning cDNA to genome
  - assembling sequence reads in genome sequencing project
  - NextGen applications: "Resequencing", ChIPSeq, etc
  - Still need to allow for discrepancies
  - due to basecalling errors & polymorphisms, introns
  - but exact match methods (hashtables, suffix arrays) do most of the work

- To detect evolutionary relationships among sequences:
  - illuminating protein structure and function via distant matches
  - illuminating *mutation* and *selection* in genomes
    - helps find non-neutrally evolving (functional) regions

Here, frequent discrepancies make finding the alignment more challenging

Often we're interested in details of alignment
 – (i.e. precisely which residues are aligned),

but

• sometimes only care whether alignment score is large enough to imply sequences are related

#### Sequences & evolution

- Similar sequences of sufficient length usually have a common evolutionary origin
  - i.e. are *homologous*
- For a pair of sequences
  - "% similarity" makes sense
  - "% homology" doesn't
- In alignment of two homologous sequences
  - differences mostly represent *mutations* that occurred in one or both lineages, but
  - Not all mutations are inferrable from the alignment

### Mutation types

- single-base substitution error by DNA polymerase
   most common type?
- strand slippage error by polymerase, inserting or deleting one or more bases
- DNA damage (radiation, or chemical) + errorprone repair, possibly altering more than one nucleotide, e.g.
  - CpG (hydrolytic deamination of methyl C)
  - dinucleotide changes, perhaps UV-induced
     dipyrimidine lesions (*Science* 287: 1283-1286)

- *Rearrangements* (break and rejoin)
  - Inversion (2 breaks on same chromosome)
  - Translocation (2 breaks on different chromosomes)
  - More complex (> 2 breaks)
- *Duplication* of a segment
- *Deletion* of a segment
- *Insertion/excision* of transposable element
- Acquisition of DNA from another organism ("*horizontal transfer*")

#### Mutation *rates* may depend on:

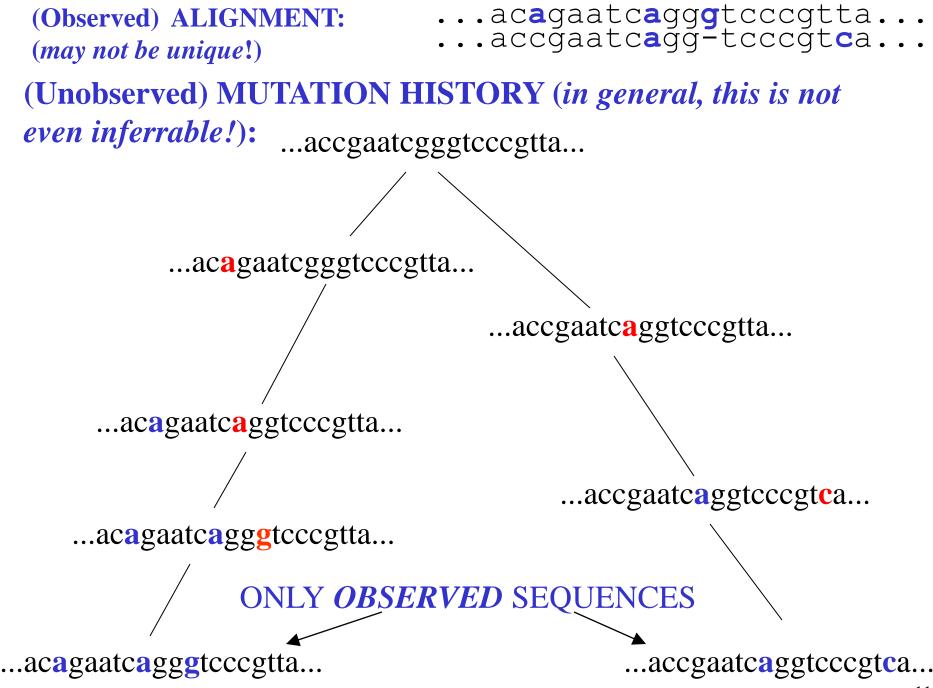
- lineage (organism): no universal "molecular clock"
- sex: e.g. in mammals, mut rate higher in males than females
- type of change e.g.
  - replacement ("substitution") of one nucleotide by another more freq than indels (insertions or deletions)
  - *transition* replacements
    - pyrimidine  $\rightarrow$  pyrimidine (T  $\leftrightarrow$  C), or purine  $\rightarrow$  purine (A  $\leftrightarrow$  G) more freq than *transversion* replacements
      - pyrimidine  $\rightarrow$  purine, or purine  $\rightarrow$  pyrimidine
  - GC or AT bias in some organisms
    - e.g.  $G \rightarrow A$  more freq than  $A \rightarrow G$  in most eukaryotes

- causes most genomes to be relatively A+T rich

- (small) deletions generally more frequent than (small) insertions

- sequence context (e.g. CpG effect)
- position in sequence some sites more slowly changing than others, due to
  - selection e.g. in coding sequences,
    - indels strongly selected against because would disrupt reading frame;
    - non-synonymous changes less freq than synonymous
  - variation in underlying mutation rate (cf. mouse genome paper)
    - may in part depend on replication timing (late replication less accurate)

- typical per base subst rates in non-coding DNA:
  - $\sim 1 \ge 10^{-9}$  per base per year (order of magnitude)
  - in humans, about  $10^{-9}$  / base / year,  $\Rightarrow 2 \ge 10^{-8}$  / base / generation  $\Rightarrow 120$  / diploid genome / generation (recent de novo estimates are lower!)
- freq of gene duplication is ~ 10<sup>-8</sup> per gene per year (*Science* 290: 1151-1155)
- freq of simultaneous dinuc substitutions is ~ 10<sup>-10</sup> per dinuc site per year (*Science* 287: 1283-1286)
- freq of CpG ⇒ TpG or CpA changes is ~10-fold higher (per CpG) than other substs in mammalian DNA;
  - may account for  $\sim 20\%$  of all substitutions.

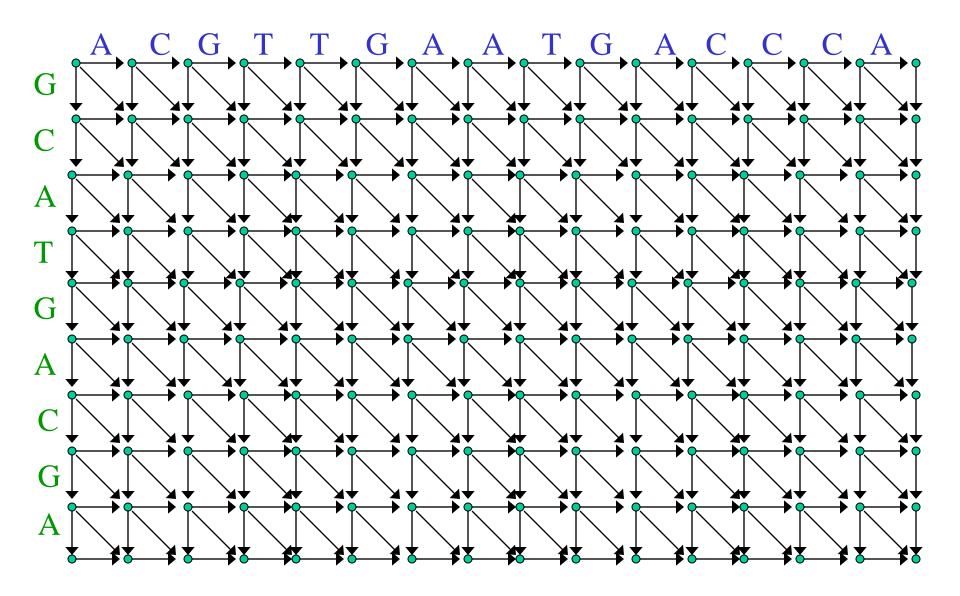


## Complications

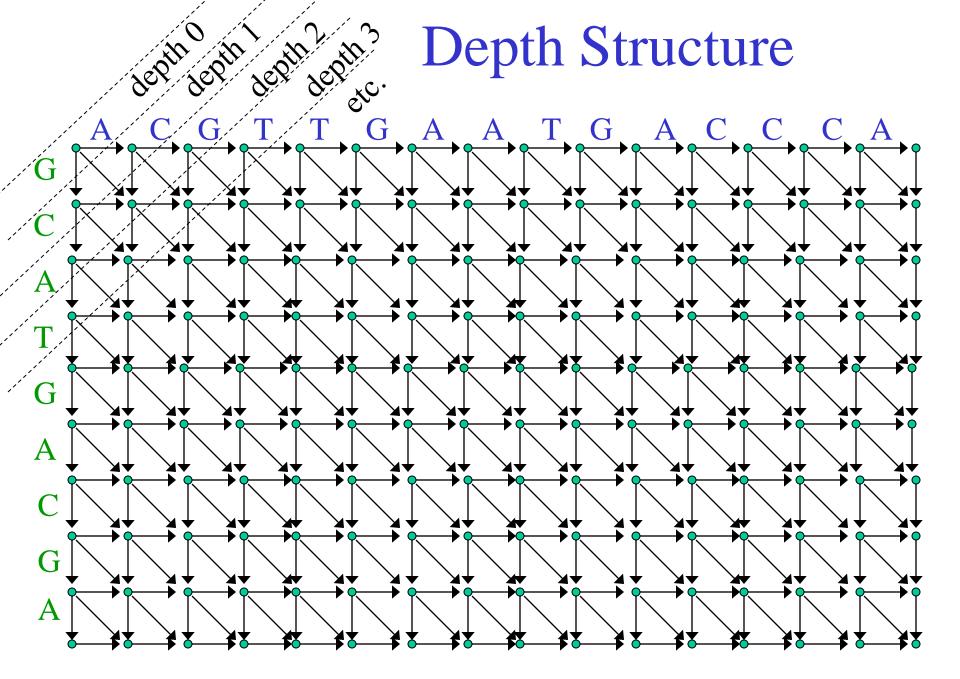
- Parallel & back mutations
  - ⇒ estimating total # of mutations requires statistical modelling
- Segmental mutations
  - duplications & other large indels
  - inversions
  - are not well modelled by alignments
    - genome-scale alignments usually done 'in pieces'

# Sequence alignments correspond to *paths* in a *DAG*!

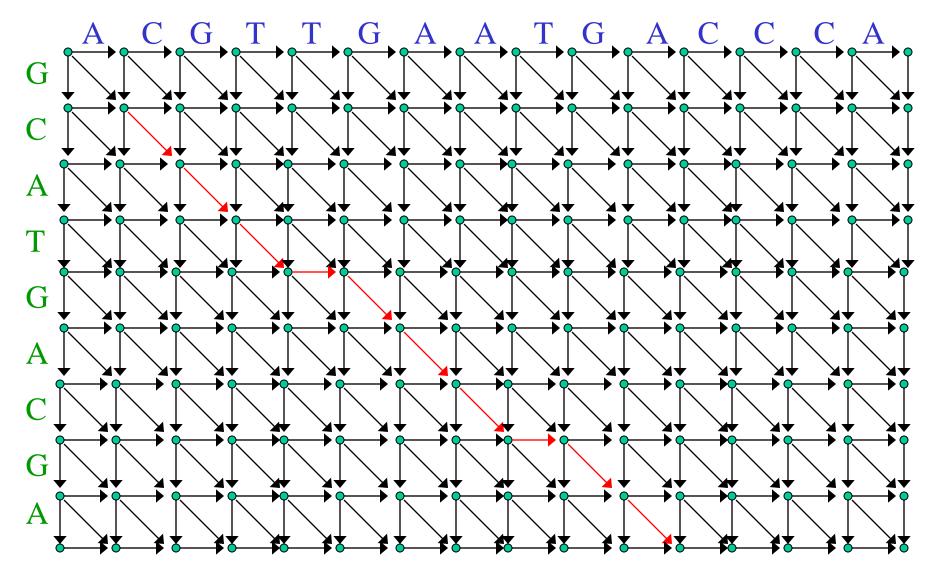
#### The Edit Graph for a Pair of Sequences



- The edit graph is a DAG.
  - Except on the boundaries, the nodes have in-degree and out-degree both 3.
- The depth structure is as shown on the next slide. Child of node of depth *n* always has
  - $\operatorname{depth} n + 1$  (for a horizontal or vertical edge), or
  - $\operatorname{depth} n + 2$  (for a diagonal edge).



- *Paths* in edit graph correspond to *alignments* of subsequences
  - each edge on path corresponds to an alignment column
  - diagonal edges correspond to column of two aligned residues
  - horizontal edges correspond to column with
    - residue in 1<sup>st</sup> (top, horizontal) sequence
    - gap in the 2<sup>d</sup> (vertical) sequence
  - vertical edges correspond to column with
    - residue in 2<sup>d</sup> sequence
    - gap in 1<sup>st</sup> sequence



Above path corresponds to following alignment (w/ lower case letters considered unaligned):

aCGTTGAATGAccca gCAT-GAC-GA

## Weights on Edit Graphs

- Edge weights correspond to scores on alignment columns.
- Highest weight path corresponds to highest-scoring alignment for that scoring system.
- Weights may be assigned using
  - a substitution score matrix
    - assigns a score to each possible pair of residues occurring as alignment column
  - or *profile* 
    - scores specific to a particular sequence

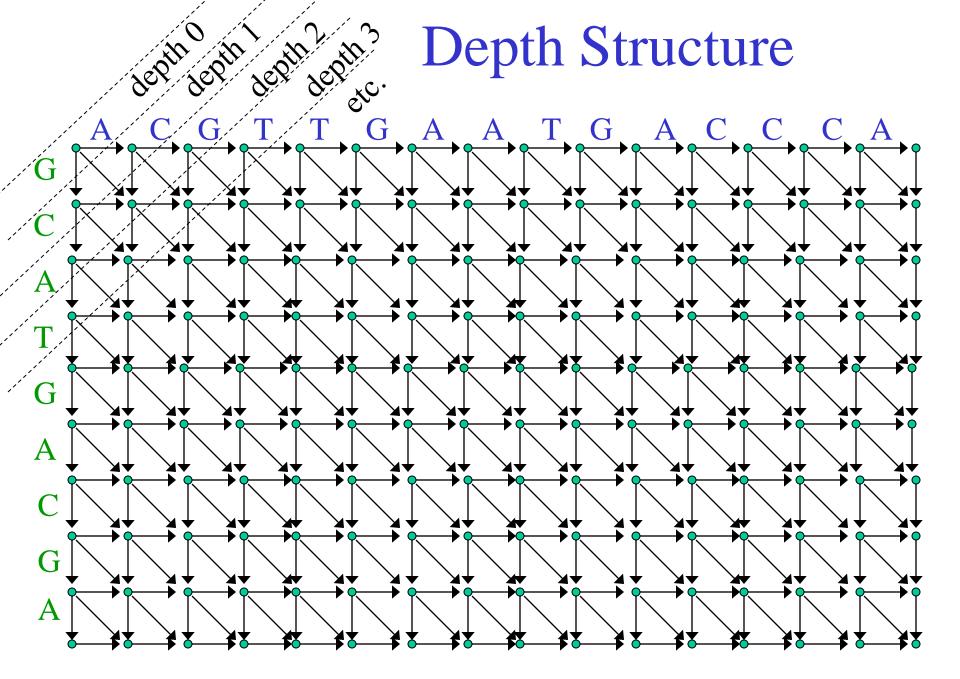
and

- a gap penalty
  - assigns a score to column consisting of residue opposite a gap.

based on appropriate probability models (next lecture!)

### Alignment algorithms

- *Smith-Waterman* algorithm to find highest scoring alignment
  - = dynamic programming algorithm to find highestweight path
    - is a *local* alignment algorithm:
      - finds alignment of subsequences rather than the full sequences.
- Can process nodes in any order in which parents precede children. Commonly used alternatives are
  - depth order
  - row order
  - column order



# Complexity

- For two sequences of lengths *M* and *N*, edit graph has
  - (M+1)(N+1) nodes,
  - 3MN+M+N edges,
- time complexity: O(MN)
- space complexity to find

highest score and beginning & end of alignment

is *O*(min(*M*,*N*))

(since only need store node's values until children processed)

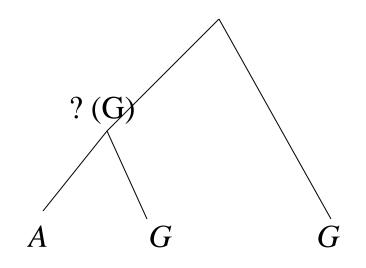
space complexity to reconstruct highest-scoring alignment:
 O(MN)

- For genomic comparisons may have
  - $-M, N \approx 10^6$  (if comparing two large genomic segments), or
  - *M* ≈ 10<sup>3</sup>, *N* ≈ 10<sup>9</sup> (if searching gene sequence against entire genome);
  - in either case  $MN \approx 10^{12}$ .
- Time complexity 10<sup>12</sup> is (marginally) acceptable.
- $\exists$  speedups which reduce constant by
  - reducing calculations per matrix cell, using fact that score often 0
    - (our program *swat*).
    - still guaranteed to find highest-scoring alignment.
  - reducing # cells considered, using nucleating word matches
    - (*BLAST*, or *cross\_match*).
    - Lose guarantee to find highest-scoring alignment.

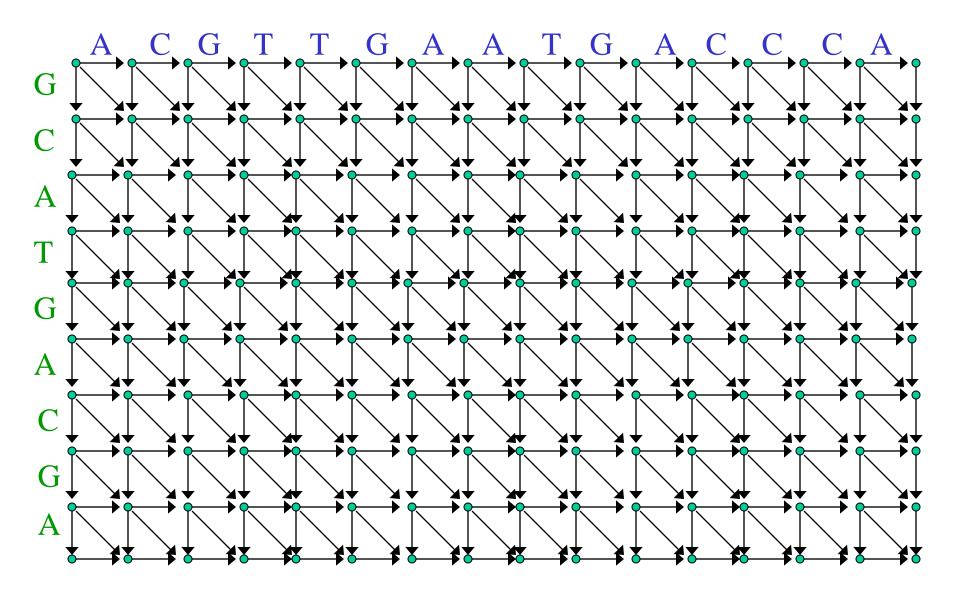
### Multiple sequence alignment

- More sequences =>
  - (potentially) more accurate alignments
  - better *resolution* of mutations, selection
- Need > 2 sequences to *polarize* mutations

• An evolutionary *tree* relates the sequences!



#### The Edit Graph for a Pair of Sequences

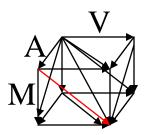


# Multiple Alignment via Dynamic Programming

- Higher dimension edit graph
  - each dimension corresponds to a sequence; co-ordinates labelled by residues
  - Each edge corresponds to aligned column of residues (with gaps).
  - Can put arbitrary weights on edges; in particular,
    - can make these correspond to probabilities under an evolutionary model (Sankoff 1975).
  - implicitly assumes independence of columns
- Highest weight path through graph again gives optimal alignment

#### Generalization to Higher Dimension

Each "cell" in 3-dimensional case looks like this:



Each edge projects onto a gap or residue in each dimension, defining an alignment column; e.g. red edge defines V

- # edges & # vertices are proportional to product of sequence lengths.
  - For k sequences of size N, is of order  $O(N^k)$ 
    - impractical even for proteins ( $N \sim 300$  to 500 residues) if k > 5:

 $300^5 = 2.4 \times 10^{12}$ 

#### Multiple alignments: paths in huge WDAGs

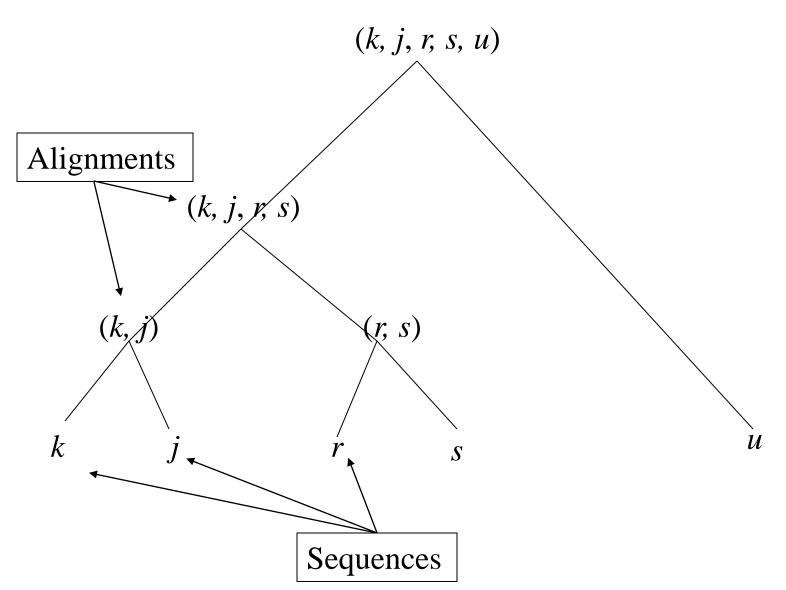
- To find high-scoring paths, need to
  - reduce size of graph
  - restrict allowed weighting schemes, and/or
  - sacrifice optimality guarantees
- Durbin *et al.* discuss methods implementing these ideas:
  - Hein
  - Carillo-Lipman
  - progressive alignment (e.g. Clustal)
- HMMs provide nice (but not guaranteed optimal) approach for constructing multiple alignments

#### Progressive alignment

- Simplest version: align one sequence (the reference) to each of the others, pairwise; construct multiple alignment from that.
- More generally, progressively align *pairs* of (*sequences or*) *alignments*, using a *guide tree* 
  - Tree may reflect evolution, or sequence quality
  - Will tend to be more accurate
- Revise gaps

- correct errors due to gap placement & gap attraction

#### Guide Tree



- Complexity: N<sup>2</sup> × (n 1) where

   N = seq length, n = # seqs
   instead of N<sup>n</sup>
- (does not count gap correction)